



UNIVERSITÀ
DEGLI STUDI
DELL'AQUILA



Extreme vertical velocity drafts as a local energy injection mechanism in stratified geophysical flows

Raffaello Foldes

PhD Student at

University of L'Aquila, *Dept. of Physical and Chemical Sciences*, (Italy),
École Centrale de Lyon - CNRS, *Lab. of Fluid Mechanics*, (France)



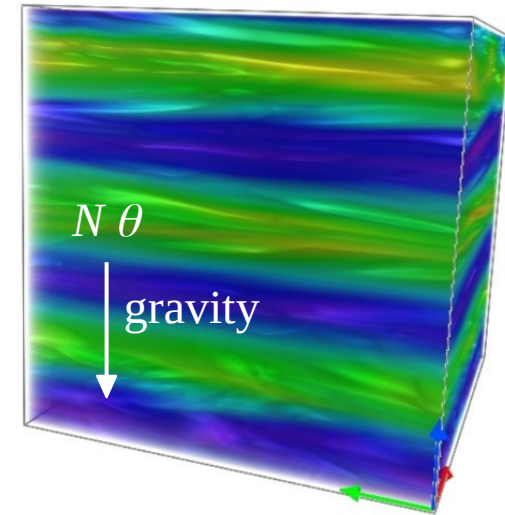
Investigating Geophysical Flows in the Boussinesq Framework

Boussinesq approximation:

$$\partial_t \bar{u} + (\bar{u} \cdot \nabla) \bar{u} = -\nabla p - N\theta \hat{z} + \mathbf{F} + \nu \nabla^2 \bar{u}$$

$$\partial_t \theta + (\bar{u} \cdot \nabla) \theta = Nw + \kappa \nabla^2 \theta; \quad \nabla \cdot \bar{u} = 0$$

Brunt-Väisälä
(gravity waves)



512³ DNS with pseudo-spectral code
(Geophysical High-Order Suite for
Turbulence, GHOST)

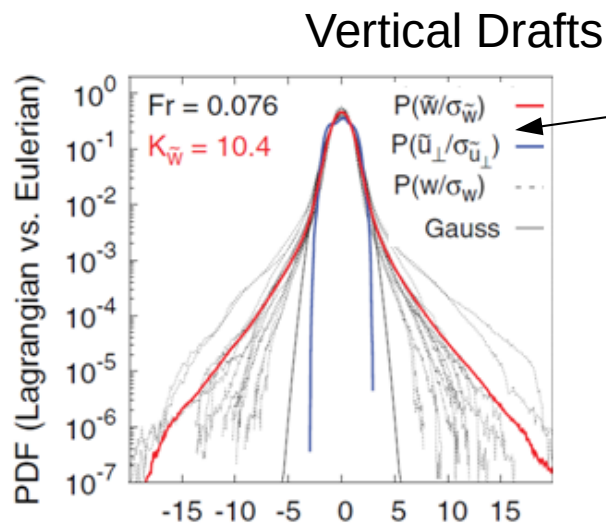
> Anisotropy (gravity)

> Competition of **Turbulence** and **Waves**

$$Re = \tau_\nu / \tau_{NL} = UL / \nu \quad \text{Reynolds number}$$

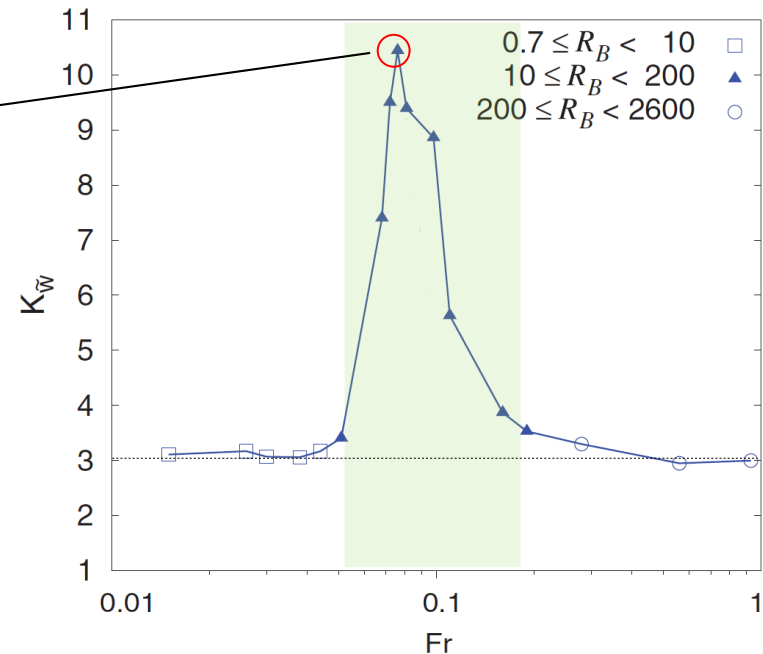
$$Fr = \tau_{W_g} / \tau_{NL} = U / LN \quad \text{Froude number}$$

$Fr \ll 1$ values of geophysical interest considered for this analysis



Resonant Intepplay
between **Turbulence**
and **Waves**

$$K_w = \frac{\langle w - \bar{w} \rangle^4}{\langle (w - \bar{w})^2 \rangle^2}$$



Filtered Energy Equations

Boussinesq approximation:

$$\partial_t \bar{u} + (\bar{u} \cdot \nabla) \bar{u} = -\nabla p - N\theta \hat{z} + \mathbf{F} + \nu \nabla^2 \bar{u} \quad (1)$$

$$\partial_t \bar{\theta} + (\bar{u} \cdot \nabla) \bar{\theta} = Nw + \kappa \nabla^2 \bar{\theta}; \quad \nabla \cdot \bar{u} = 0 \quad (2)$$

Filtering the equations and multiplying eq. 1 by \tilde{u} and eq. 2 by $\tilde{\theta}$

Filtered Kinetic Energy Eq.

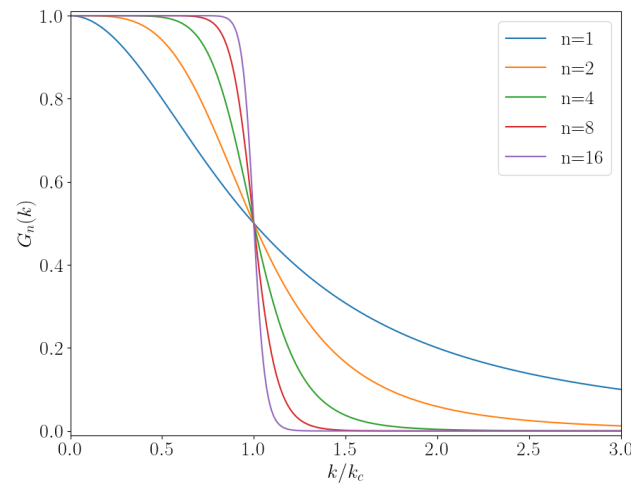
$$\partial_t \langle \tilde{\mathcal{E}}_u \rangle = -N \langle \tilde{\theta} \tilde{w} \rangle + \langle \mathcal{S}_u \rangle + \langle \tilde{D}_\nu \rangle + \langle \tilde{\epsilon}_{ext} \rangle$$

Filtered Potential Energy Eq.

$$\partial_t \langle \tilde{\mathcal{E}}_\theta \rangle = N \langle \tilde{\theta} \tilde{w} \rangle + \langle \mathcal{S}_\theta \rangle + \langle \tilde{D}_\kappa \rangle$$

Butterworth (low-pass) filter

$$G_n(k) = 1 / [1 + (k/k_c)^{2n}]$$

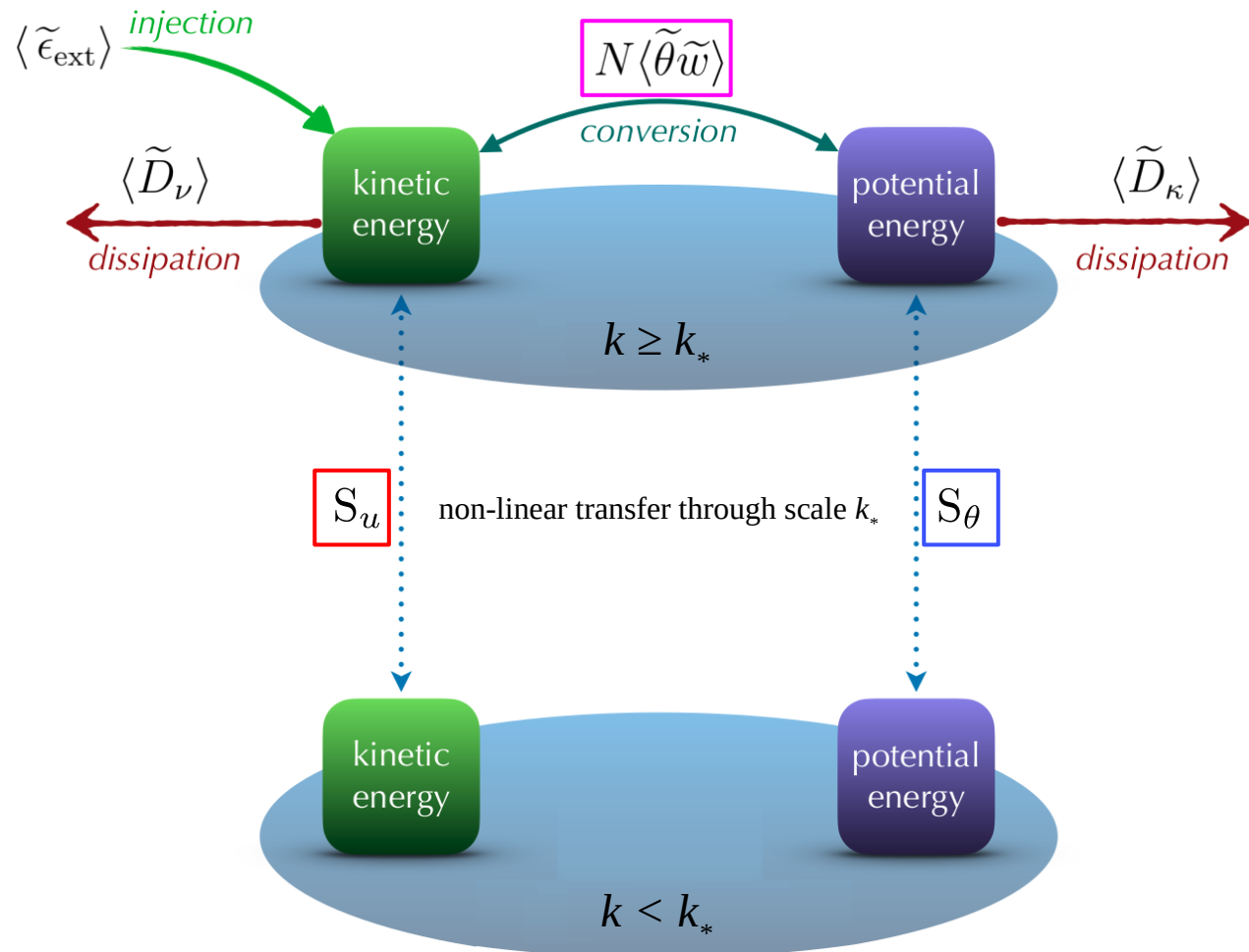


$$\tilde{\mathbf{v}}(\mathbf{x}, t) \doteq \int_V G(\mathbf{x} - \xi) \mathbf{v}(\xi, t) d^3 \xi$$

$$k \doteq k_\perp = \sqrt{k_x^2 + k_y^2} \quad \text{Axisymmetric}$$

k_* is the Filtering Scale

Sub-grid terms are defined in (real) physical space.



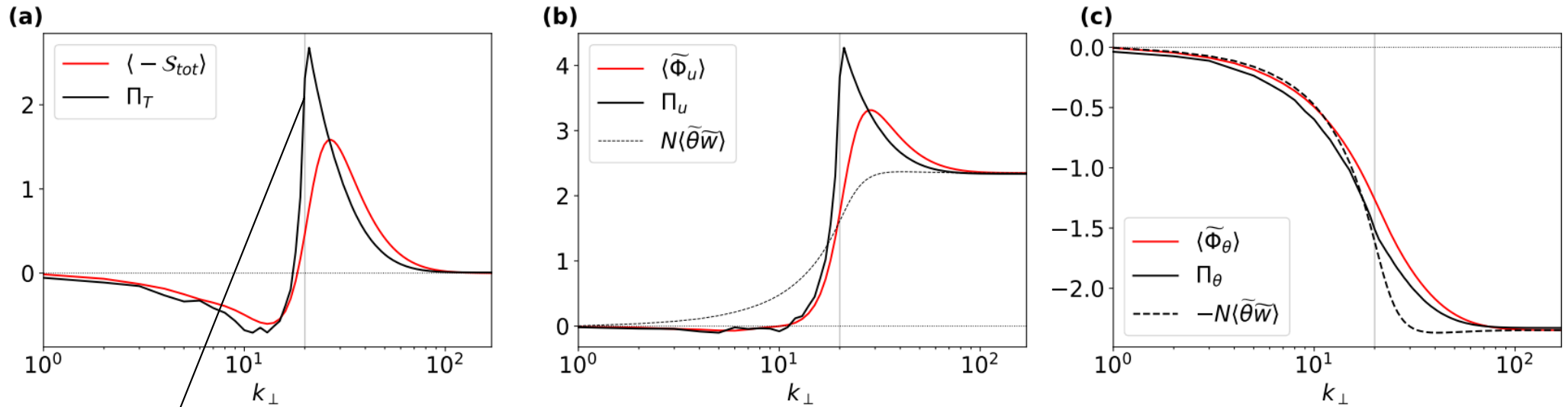
from Foldes et al., (in preparation)

Sub-Grid terms as a Proxy for the Perpendicular Fourier Flux

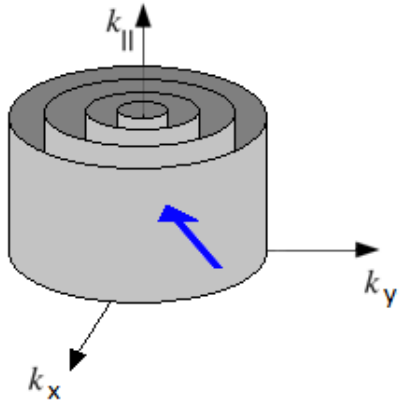
Run I: 512^3 , $L_0 = 2\pi$ (triply periodic), $Re = 97$, $k_F = 20$, $Fr = 0.128$ (no drafts)

Total Kinetic/Potential Energy Transfer: $\Phi_{u,\theta} = \langle -\mathcal{S}_{u,\theta} \rangle \pm N \langle \tilde{\theta} \tilde{w} \rangle$

“Classical” Fourier Energy Flux: $\Pi_{u,\theta,T}$



from Foldes et al., (in preparation)



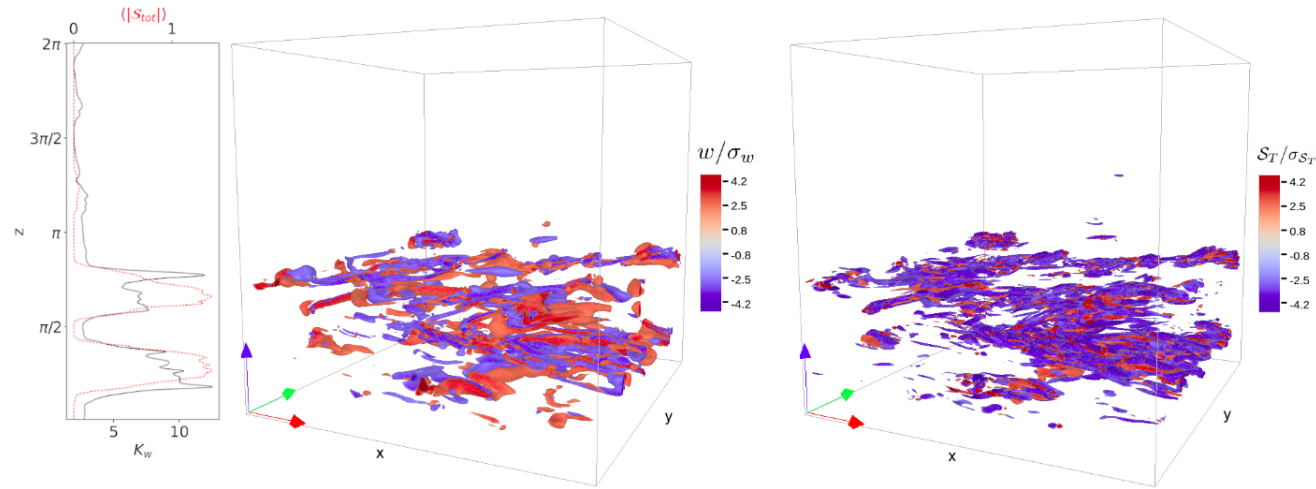
- (a) Sub-grid term is able to recover the major features of the classical Fourier flux
- (b) Kinetic energy transfer is always from large to small scales
- (c) Potential energy transfer is always negative *but* dominated by the conversion of energy from kinetic to potential

→ Perpendicular Fourier Flux ↔ Axisymmetric Sub-grid terms

Vertical Drafts as an Energy Injection Mechanism I

Run I: 512^3 , $L_0 = 2\pi$ (triply periodic), $Re = 3800$, $k_F = 2/3$, $Fr = 0.076$ (*drafts*)

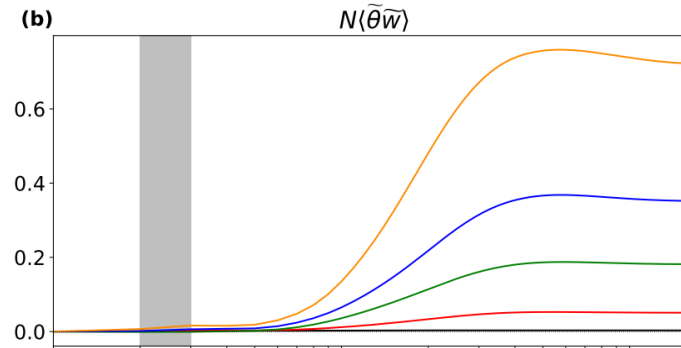
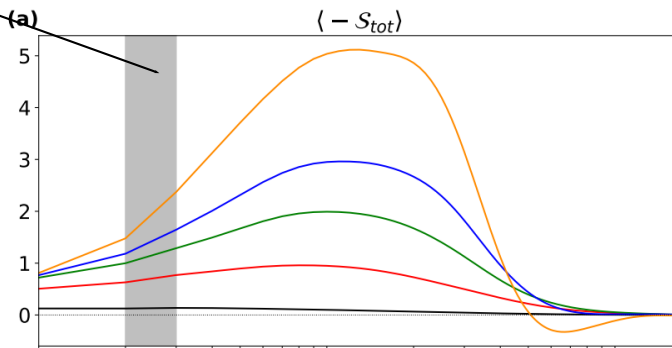
- Net total (and kinetic) energy transfer from large to small scales with a wide peak at $7 \leq k \leq 30$
- In the same range there is a significant conversion of energy from kinetic to potential
- Potential energy see *drafts* as an external energy injection mechanism



from Foldes et al., (in preparation)

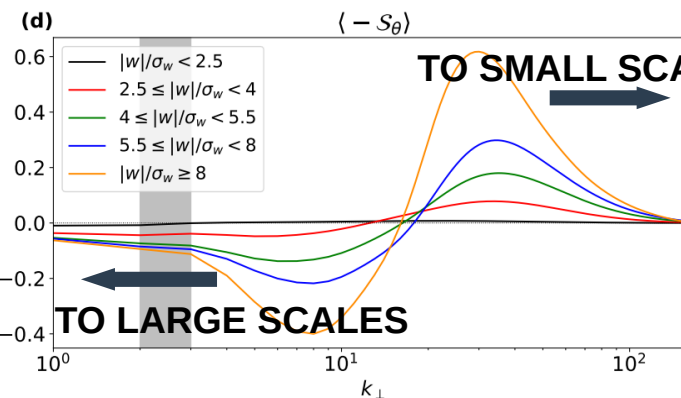
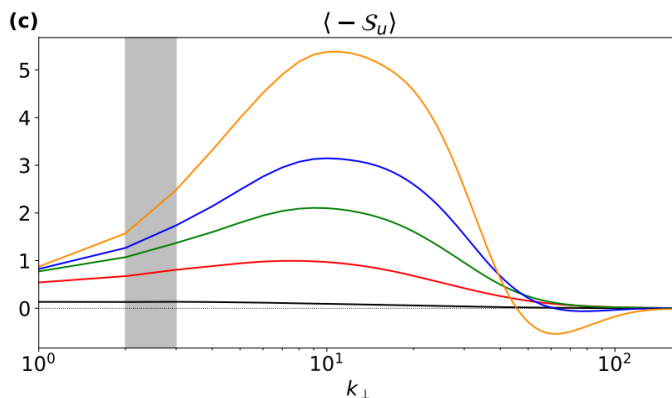
Forcing scales

Filtered Total Energy



Conversion term

Kinetic Sub-grid term

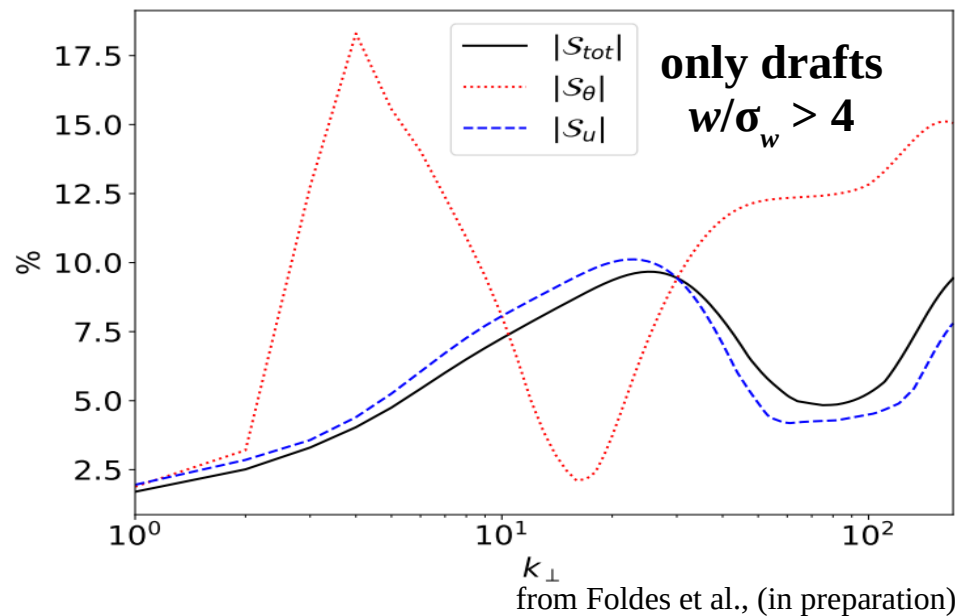


Energy locally injected by vertical drafts?

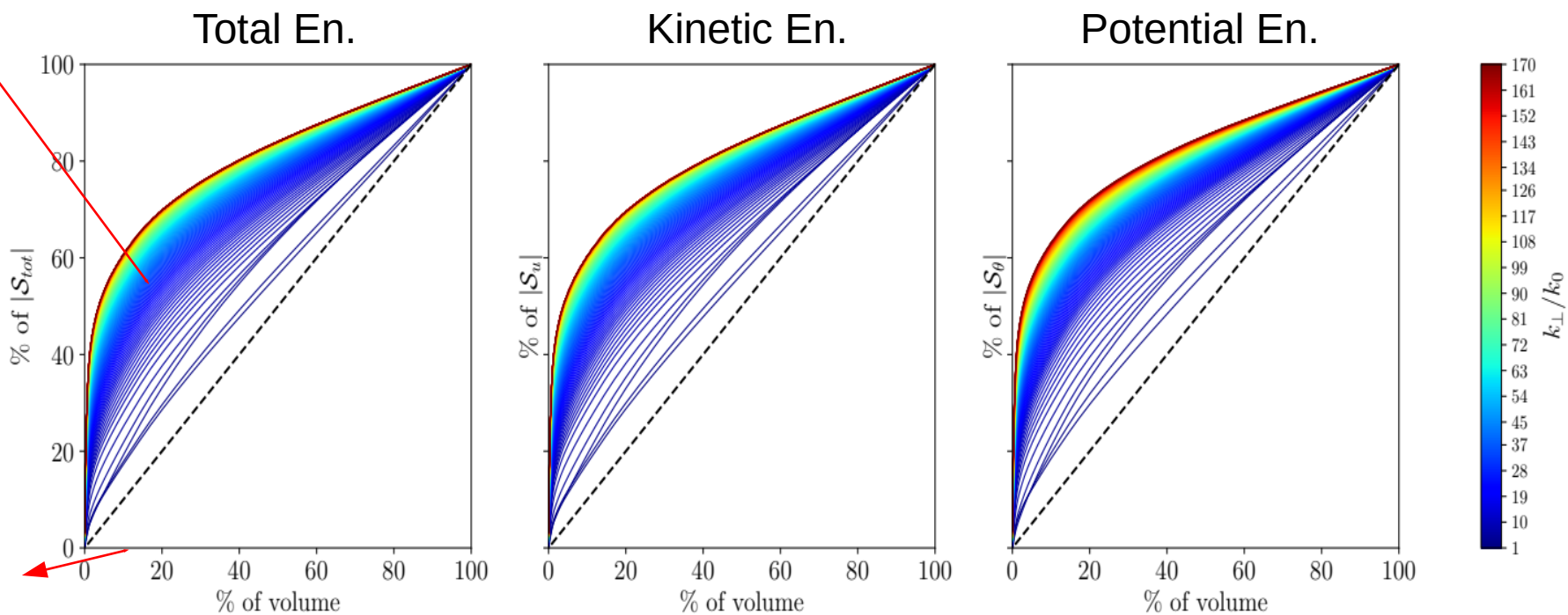
Potential Sub-grid term

Vertical Drafts as an Energy Injection Mechanism II

- At $k > 30$, less than 10% of volume transfers more than 50% of energy
- In particular a tiny percentage of the volume ($\sim 0.02\%$) transfers 5-10% of kinetic energy and up to $\sim 15\%$ of potential



> 50% of energy transfer



10% of volume

Thank you for your attention!

Conclusions

- Stratified flows develop extreme vertical drafts in a range of parameters of geophysical interest, making the flow inhomogeneous
- To investigate the feedback of these extreme events on the dynamics and the energetics of the flow we implemented a space-filtering approach on the Boussinesq equations
- We identified a way to obtain a proxy of the energy flux which is local in the physical space and provides information of the same type to those of the classical perpendicular energy flux integrated in cylindrical shells in the Fourier space
- We found that an enhanced energy transfer is associated to a specific range of wave vector which is likely to correspond with the scale of the emerging extreme drafts
- A strong coupling occurs in presence of extreme drafts between kinetic and potential energy, representing a forcing mechanism for the potential temperature field
- This coupling produces a dual transfer of potential energy to small and large scale around $k = 20$